





# Finite Element Model of the Switched Reluctance Machine with FEMM and Matlab – Part 1

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# 1. Requirements

• FEMM 4.2 (download: www.femm.info)

## 2. Introduction

In this document, we present a step-by-step tutorial to simulate a switched reluctance machine (SRM) with FEMM. Although the objective of the tutorial is for the reader to build the model on their own, the completed tutorial\_SRM\_QUEVAL\_20210201.fem can also be downloaded.

## 3. Model construction

The SRM to be analyzed is pictured in Figure 1. It has 8 stator teeth and 6 rotor teeth (SRM 8-6). The rotor has an outer diameter of ~68 mm. The airgap width is 0.4 mm. The stator has an outer diameter of 143 mm. The axial length of the machine is 200 mm. There are 4 coils (a, b, c, d), each wound with 18 turns of copper wire. For the purposes of this example, we will consider the case in which a steady current of 50 A is flowing through the coil c.

In FEMM, one models the 2D problem using symmetry conditions to reduce the problem complexity. By convention, positive-valued currents flow in the out-of-the-page direction and positive-valued rotation is in the counterclockwise direction.



Figure 1 - SRM geometry and conventions.

## 3.1 Create a new model

Run the FEMM application. The default preferences will bring up a blank window with a minimal menu bar.

Select File > New from the main menu. A dialog will pop up with a drop list allowing you to select the type of new document to be created. Select Magnetics Problem and hit the OK button. A new blank magnetics problem will be created, and several new toolbar buttons will appear.

## 3.2 Set problem definition

The first task is to tell the program what sort of problem is to be solved. To do this, select Problem from the main menu. The Problem Definition dialog appears. Set Problem Type to Planar. Make sure that Length Units is set to Millimeters and that the Frequency is set to 0. Set the Depth to 200. Set the Smart Mesh to Off (Figure 2). Hit the OK button.

| Problem Type      | Planar       | - |
|-------------------|--------------|---|
| Length Units      | Millimeters  | • |
| Frequency (Hz)    | 0            |   |
| Depth             | 200          |   |
| Solver Precision  | 1e-008       |   |
| Min Angle         | 30           |   |
| Smart Mesh        | Off 💽        |   |
| AC Solver         | Succ. Approx |   |
| Previous Solution |              |   |
| Prev Type         | None         |   |
| Comment           |              |   |
| Add comments      | here.        |   |

Figure 2 - "Problem definition" dialog.

# 3.3 Draw the SRM

We will first draw the rotor, then the stator. Then we will cut the full geometry to obtain the half geometry.

# 3.3.1 Rotor

Select the Operate on nodes button , so that nodes can be drawn. One can place nodes either by moving the mouse pointer to the desired location and pressing the left mouse button, or by pressing the <TAB> key and manually entering the point coordinates via a popup dialog. Place nodes at the coordinates given in Table 1. Click on Zoom extents to adapt the view to your screen. The result is shown on Figure 3.

| Node | x [mm] | y [mm] |
|------|--------|--------|
| A    | 11.5   | 0      |
| В    | -11.5  | 0      |
| С    | 20     | 6.08   |
| D    | 20     | -6.08  |
| E    | 33.35  | 6.08   |
| F    | 33.35  | -6.08  |

Table 1 - Rotor nodes coordinates



Figure 3 – Rotor geometry after plotting the nodes of Table I.

Draw the circle of diameter [AB]. Do do so, select the Operate on arc segments button By selecting two nodes with left mouse button clicks in sequence, one can obtain arcs between them. Select the node A, then the node B. The Arc segment properties dialog appears. Set the Arc Angle to 180, and click OK. An arc segment is obtained. Select the node B, then the node A. The Arc segment properties dialog appears. Set the Arc Angle to 180, and click OK. Another arc segment is obtained. The two arcs form the circle of diameter [AB].

NOTE: An arc segment is always plotted counterclockwise with respect to the origin (0,0) starting from the first point that is added.

Draw the segments [CE] and [DF]. To do so, select the Operate on segments button  $\checkmark$  so that lines can be drawn connecting the nodes. By selecting the nodes defining the coil with left mouse button clicks in sequence, one obtains segments between each of the nodes. Select the node C, then the node E. The segment [CE] is obtained. Select the node D, then the node F. The segment [DF] is obtained. The result is shown on Figure 4.



Figure 4 – Rotor geometry after plotting the circle and the segments.

Select the Operate on segments button . Right click on the segments [CE] and [DF], they will turn red, denoting that they are selected. Select the Copy selected objects button . The Copy dialog appears. Select Rotation. Set the Angular shift to 60 degrees and the Number of copies to 5. Click OK. The result is shown on Figure 5.



Figure 5 – Rotor geometry after rotating the segments.

Select the Operate on arc segments button . Draw the arc segments shown on Figure 6. Set the Arc Angle to 26 for the inner arcs. Set the Arc Angle to 21 for the outer arcs. The result is shown on Figure 6.



Figure 6 - Rotor geometry after plotting the arcs.

The drawing of the rotor is finished. Save the model.

#### 3.3.2 Stator

Let's move the rotor on the side, to have more space to draw the stator. Select the Operate on groups of objects button . Select the Select a group of entities using the mouse button . Select all the rotor, it will turn red, denoting that it is selected. Select the Move/Rotate selected objects button . The Move dialog appears. Select Translation. Set the horizontal shift to 200. Click OK. The rotor moves to the right.

Switch to Nodes mode by pressing the Operate on nodes button . Place nodes at the coordinates given in Table 2. The result is shown on Figure 7.

| Node | x [mm] | y [mm] |
|------|--------|--------|
| G    | 34.3   | 0      |
| Н    | 53.4   | 0      |
|      | 51.3   | 14.9   |
| J    | 51.3   | -14.9  |
| К    | 33.5   | 7.5    |
| L    | 33.5   | -7.5   |
| М    | 71.5   | 0      |
| N    | -71.5  | 0      |

Table 2 - Stator nodes coordinates



N •

Figure 7 - Stator geometry after plotting the points of Table II.

+

Draw the circle of diameter [MN].

Draw the segments [GH], [KI] and [LJ].

Select the Operate on arc segments button . Draw the arc segments (LG and (GK with the Arc Angle set to 12.6 degrees. Draw the arc segments (JH and (HI with the Arc Angle set to 16.2 degrees. The result is shown on Figure 8.



Figure 8 - Stator geometry after plotting the circle, the segments and the arcs.

Select the Operate on a group of objects button . Left click on the Select a group of entities using the mouse button . Select the segments [GH], [KI] and [LJ] and the arcs (KG, (GL, (IH and (HJ. They will turn red, denoting that they are selected. Select the Move/Rotate selected objects button . The Move dialog appears. Select Rotation. Set the Angular shift to 22.5 degrees. Click OK.

Select the Operate on a group of objects button . Left click on the Select a group of entities using the mouse button . Select the segments [GH], [KI] and [LJ] and the arcs (KG, (GL, (IH and (HJ. They will turn red, denoting that they are selected. Select the Copy selected objects button . The Copy dialog appears. Select Rotation. Set the Angular shift to 45 degrees and the Number of copies to 7. Click OK. The result is shown on Figure 9.



Figure 9 - Stator geometry after moving + rotating the segments and the arcs.

Select the Operate on arc segments button . Draw the arc segments shown on Figure 10 with the Arc Angle set to 18.8 degree. The result is shown on Figure 10.

The drawing of the stator is finished. Save the model.



Figure 10 - Stator geometry after plotting the arcs.

#### 3.3.3 Full geometry

Let's move the rotor back to the center. Select the Operate on groups of objects button Select the Select a group of entities using the mouse button . Select all the rotor, it will turn red, denoting that it is selected. Select the Move/Rotate selected objects button . The Move dialog appears. Select Translation. Set the horizontal shift to -200. Click OK. The result is shown on Figure 11.



Figure 11 - Full geometry.

Let's add two circles in the airgap that will be used to deal with the rotation. Switch to Nodes mode by pressing the Operate on nodes button . Place nodes at the coordinates given in Table 3. Draw the circle of diameter [PQ] and the circle of diameter [RS]. The result is shown on Figure 12.

| Node | x [mm] | y [mm] |
|------|--------|--------|
| Р    | 34     | 0      |
| Q    | -34    | 0      |
| R    | 34.2   | 0      |
| S    | -34.2  | 0      |

Table 3 - Airgap nodes coordinates



Figure 12 - Zoom on the airgap after plotting the 2 circles in the airgap.

#### 3.3.4 Half geometry

Thanks to the symmetries, we need to model only half the geometry. Select the Operate on segments button  $\checkmark$ . Draw the segment [MN]. The result is shown on Figure 13. Observe that new points have been automatically added at the intersections (Figure 14).



Figure 13 - Full geometry after plotting the segment [MN].



Figure 14 - Zoom on the airgap after plotting the segment [MN]. The new points that are automatically added at the intersections between [MN] and previously existing segments or arcs are denoted "new".

Select the Operate on segments button  $\checkmark$ . Select all the segments of the bottom half of the geometry and click on the Delete selected objects button  $\Join$ . Select the Operate on arc segments button  $\frown$ . Select all the segments of the bottom half of the geometry and click on the Delete selected objects button  $\Join$ . Select the Operate on nodes button  $\boxdot$ . Select all the nodes of the bottom half of the geometry and click on the Delete selected objects button  $\Join$ . Select the Operate on nodes button  $\boxdot$ . Select all the nodes of the bottom half of the geometry and click on the Delete selected objects button  $\Join$ . The result is shown on Figure 15.



Figure 15 - Half geometry.

Select the Operate on segments button  $\square$ . Select the segments [AB], [PR] and [QS] and click on the Delete selected objects button  $\bowtie$ . The result is shown on Figure 16 and Figure 17.



Figure 16 - Half geometry after deleting the segments.



Figure 17 - Zoom on the airgap after deleting the segments.

The drawing of the geometry is finished. Save the model.

## **3.4 Add materials to the model**

Select Properties > Materials Library from the main menu. The Materials Library dialog appears. Drag-and-drop Air from Library Materials to Model Materials to add it to the current model. Go into the Soft Magnetic Materials > Silicon Iron folder and drag M-19 Steel into Model Materials. Click on OK.

## 3.5 Add circuits to the model

Select Properties > Circuits from the main menu. The Property Definition dialog opens.

Push the Add Property button to create a new circuit property. In the Circuit Property dialog, set the Name to a. Specify that the circuit property is to be applied to a wound region by making sure that the Series radio button is selected. Set the Circuit Current to 0. Click on OK.

Push the Add Property button to create a new circuit property. In the Circuit Property dialog, set the Name to b. Specify that the circuit property is to be applied to a wound region by making sure that the Series radio button is selected. Set the Circuit Current to 0. Click on OK.

Push the Add Property button to create a new circuit property. In the Circuit Property dialog, set the Name to c. Specify that the circuit property is to be applied to a wound region by making sure that the Series radio button is selected. Set the Circuit Current to 50. Click on OK (Figure 18).

| Circuit Prope | ty            |          | ×      |
|---------------|---------------|----------|--------|
| Name C        |               |          |        |
| C Parallel    | Circuit Curre | nt, Amps |        |
|               |               | ОК       | Cancel |
|               |               |          | -      |

Figure 18 – "Circuit property" dialog for circuit c.

Push the Add Property button to create a new circuit property. In the Circuit Property dialog, set the Name to d. Specify that the circuit property is to be applied to a wound region by making sure that the Series radio button is selected. Set the Circuit Current to 0. Click on OK. Click on OK to close the Property Definition dialog.

#### **3.6 Place block labels**

FEMM uses block labels to associate materials and other properties with various domains in the problem geometry.

Select the Operate on Block Labels button . In the same way as nodes, block labels can be placed either by a click on the left mouse button, or via the <TAB> dialog. Place a block label in each one of the 12 domains. Make sure that the labels in the Airgap stator side domain and in the Airgap rotor side domain are correctly located. The result is shown on Figure 19 and Figure 20.

*NOTE:* If snap-to-grid  $\leq$  is enabled then it may be sometimes difficult to place the block label in the empty space. If this is the case, disable snap-to-grid by de-selecting the button  $\leq$ .



Figure 19 - Half geometry after adding the block labels.



Figure 20 - Zoom on the airgap after adding the block labels. Note that there is one label in the airgap stator side domain and one label in the airgap rotor side domain. There is no label in the domain between them.

## 3.7 Associate a material and a circuit property to each domain

We want to associate each domain (Figure 21) to its material and circuit properties, as defined in Table 4. This is done using the block label placed in each domain. For the sake of example, let's consider the Coil b+ domain.



Figure 21 - Half geometry with coil domains definitions.

| Domain             | Block type | Mesh size | In circuit    | In group |
|--------------------|------------|-----------|---------------|----------|
|                    |            |           | (turns)       |          |
| Coil b+            | Air        | 2         | b (18)        | 0        |
| Coil b-            | Air        | 2         | b (-18)       | 0        |
| Coil c+            | Air        | 2         | c (18)        | 0        |
| Coil c-            | Air        | 2         | c (-18)       | 0        |
| Coil d+            | Air        | 2         | d (18)        | 0        |
| Coil d-            | Air        | 2         | d (-18)       | 0        |
| Coil a-            | Air        | 2         | a (-18)       | 0        |
| Stator iron        | M-19 Steel | 2         | <none></none> | 0        |
| Airgap stator side | Air        | 0.2       | <none></none> | 0        |
| Airgap rotor side  | Air        | 1         | <none></none> | 0        |
| Rotor iron         | M-19 Steel | 2         | <none></none> | 10       |

Table 4 - Material and circuit property of each domain

Right click on the block label node in the Coil b+ domain. The block label will turn red, denoting that it is selected. Press <SPACE> to "open" the selected block label (Instead of pressing the space bar, one can use the Open up Properties Dialog toolbar button 🖆). The Properties for selected block dialog will pop up, containing the properties assigned to the selected label.

Set the Block type to Air.

Uncheck the Let Triangle choose Mesh Size checkbox and set the Mesh size to 2. The mesh size parameter defines a constraint on the largest possible elements size allowed in the associated section. The mesher attempts to fill the region with nearly equilateral triangles in which the sides are approximately the same length as the specified Mesh size parameter.

We want to assign currents to flow in this region, so select b from the In Circuit drop list. The Number of turns edit box will become activated if a series-type circuit is selected for the region (the Coil property that was previously defined). Enter 18 as the number of turns for this region, denoting that the region if filled with 18 turns with positive-valued currents flowing in the out-of-the-page direction.

Click on OK. The block label is then be labeled as Air[b:18].

NOTE: If we wanted to denote that the turns have positive-valued currents flowing in the intothe-page direction instead, we would have specified the number of turns to be -18. The block label would then be Air[b:-18].

Similarly define the other domains according to Table 4. Note that there are two a- domains. The result is shown on Figure 22.



Figure 22 - Half geometry after associating material and circuit property to each domain.

At this point, all the domain materials and circuit properties have been defined. Save the model.

# 3.8 Add boundary conditions to the model

Select Properties > Boundary from the main menu.

Push the Add Property button. The Boundary Property dialog opens. Set the Name to zero. Specify that the boundary property is a Dirichlet boundary condition by selecting Prescribed A in the BC Type field. Click on OK (Figure 23).

Push the Add Property button. The Boundary Property dialog opens. Set the Name to move. Specify that the boundary property is an anti-periodic boundary condition by selecting Anti-periodic Air Gap in the BC Type field. Click on OK (Figure 23).

Push the Add Property button. The Boundary Property dialog opens. Set the Name to pl. Specify that the boundary property is an anti-periodic boundary condition by selecting Anti-periodic in the BC Type field. Click on OK (Figure 23). In the same manner, create anti-periodic boundary conditions p2, p3 and p4.

Click on OK to close the Property Definition dialog.



"zero"

"move"

Figure 23 - "Boundary Property" dialogs.

#### 3.9 Associate a boundary condition to each model boundary

We want to associate each boundary (Figure 24 and Figure 25) to its boundary condition.

Switch to Arc segment mode by pressing the Operate on arc segments toolbar button 🗅.

Right click on the outer iron boundary. The boundary will turn red, denoting that it is selected. Press <SPACE> to "open" the selected arc (Instead of pressing the space bar, one can use the Open up Properties Dialog toolbar button 2). A dialog will pop up containing the properties assigned to the selected arc. Set the Max. segment, Degree to 5. Set the Boundary cond. to zero. Click OK.

Similarly assign the zero boundary condition to the inner iron boundary, with the Max. segment, Degree set to 5.

Similarly assign the move boundary condition to the inner and outer airgap boundaries, with the Max. segment, Degree set to 1.

Switch to Segment mode by pressing the Operate on segments toolbar button 🗹.

Right click on the p1 boundary. The boundary will turn red, denoting that it is selected. Press <SPACE> to "open" the selected segment (Instead of pressing the space bar, one can use the Open up Properties Dialog toolbar button 2. A dialog will pop up containing the properties assigned to the selected segment. Set the property to p1. Click OK.

Similarly assign the p1 boundary condition to the p1' boundary.

Similarly assign the p2 boundary condition to the p2 and p2' boundaries.

Similarly assign the p3 boundary condition to the p3 and p3' boundaries.

Similarly assign the p4 boundary condition to the p4 and p4' boundaries.

At this point, all the boundary conditions have been defined. Save the model.



Figure 24 - Half geometry with boundary definitions.



Figure 25 - Zoom on the airgap with boundary definitions.

## 4. Generate Mesh

Click on the toolbar button with yellow mesh 🖾. This action generates a triangular mesh for your problem (Figure 26). You should have approximately 9400 nodes.

NOTE: If the mesh spacing seems to fine or too coarse you can select block labels or line segments and adjust the Mesh size defined in the properties of each object. To adjust all of the mesh sizes in your model at once, press <F3> to refine the mesh in all blocks or <F4> to coarsen the mesh in all blocks. Then you can regenerate the mesh.



Figure 26 - Half geometry after generating the mesh.

# 5. Run the finite element analysis

Click on the "turn the crank" button 📽 to analyze your model.

Processing status information will be displayed. If the progress bars do not seem to be moving then you should probably cancel the calculation. This can occur if insufficient boundary conditions have been specified. For this particular problem, the calculations should be completed within a second. There is no confirmation for when the calculations are complete, the status window just disappears when the processing is finished.

## 6. Analysis Results

Click on the glasses icon 🖄 to view the analysis results. A post-processor window will appear. The post-processor window will allow you to extract many different sorts of information from the solution. By default, a black-and-white graph of flux lines is displayed (Figure 27).



Figure 27 – Default analysis results: flux lines.

#### 6.1 Getting field values at a point

Just like the pre-processor, the post-processor window has a set of different editing modes: Point , Contour , and Area . In Point mode, by clicking on any point with the left mouse button, the various field properties associated with that point are displayed in the floating FEMM Output window. Similar to drawing points in the pre-processor, the location of a point can be precisely specified by pressing the <TAB> button and entering the coordinates of the desired point in the dialog that pops up. For example, for the point (0, 45), the FEMM Output dialog is shown in Figure 28. You should obtain a similar result (but probably not exactly the same values).

*Note: If the* FEMM Output *dialog disappeared, select* View > Output windows *from the main menu.* 



Figure 28 – "FEMM Output" dialog for the point (0, 45).

#### 6.2 Plotting field values along a contour

FEMM can also plot values of the field along a user-defined contour. Here, we will plot the magnetic flux density along the centerline of the coil. Switch to Contour mode by pressing Contour 2. You can now define a contour along which flux will be plotted. There are three ways to add points to a contour:

1. Left Mouse Button Click adds the nearest input node to the contour;

2. Right Mouse Button Click adds the current mouse pointer position to the contour;

3. <TAB> Key displays a point entry dialog that allows you to enter in the coordinates of a point to be added to the contour.

Here, method 3 can be used. Press  $\langle TAB \rangle$ , add the point (-12, 45), then add the point (12, 45). Then, press the Plot toolbar button  $\square$ . The x-y Plot of Field Values dialog opens (Figure 29). The default selection is |B| (Magnitude of flux density). If desired, different types of plot can be selected from the drop list on this dialog. Hit OK. The results are shown in Figure 30.

| Plot Type                   |        |
|-----------------------------|--------|
| B (Magnitude of flux densit | y) 🔻   |
| Number of points in plot    |        |
| 1500                        | OK     |
|                             | Cancel |
| File Formatting             |        |

Figure 29 - "X-Y plot field values" dialog.



Figure 30 - Plot of the flux density along the axis of the coil c.

Note: It is often the case in the solution to magnetic problems that the field values are discontinuous across a boundary. In this case, FEMM determines which side of the boundary will be plotted based on the order in which points are added. For example, if points are added around a closed contour in a counterclockwise order (with respect to the origin), the plotted points will lie just to the inside of the contour. If the points are added in a clockwise order, the plotted points will lie just to the outside of the contour.

# 6.3 Plotting Flux Density

To make a color density plot of the magnetic flux density, click on the rainbow-shaded toolbar button S. When the dialog box comes up, select the Show Density Plot radio button and accept the other default values. Click on OK. The resulting solution is shown in Figure 31.



Figure 31 – Plot of the flux density distribution.

# 7. Conclusions

You have now completed the finite element modeling of a SRM with FEMM (part 1). In this tutorial, you learned how to:

- Draw a geometry using nodes, segments and arcs;
- Define the material and circuit properties;
- Define the boundary conditions;
- Generate a mesh;
- Run the analysis;
- Inspect local field values;
- Plot field values along a contour;
- Display color flux density plots.